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Design and Assembly Analysis of a Worm-Assembly in a Gear Box

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ABSTRACT:

Differential is a part of inner axle housing assembly, which includes the differential rear axles, wheels and bearings. The differential consists of a system of gears arranged in such a way that connects the propeller shaft with the rear axles. Worm gear speed reducers are comprised of the terms "gearbox" and "speed reducer" that are used interchangeably in the world of power transmission and motion control. Gearboxes are used for speed reduction and torque multiplication. A hybrid term of "gear reducer" is also commonly used when talking about gearboxes. This is simply a gearbox (or speed reducer, or gear reducer) with a motor directly mounted to the input. A gearbox designed using a worm and worm-wheel will be considerably smaller than one made from plain spur gears and has its drive axes at 90° to each other. With a single start worm, for each 360° turn of the worm, the worm-gear advances only one tooth of the gear. In the present work all the parts of differential are designed under Structural condition and modeled. The required data is taken from journal paper. Modeling and assembly is done in Solid Works. The detailed drawings of all parts are to be furnished. The main aim of the project is to focus on the mechanical design and contact analysis on assembly of gears in gear box when they transmit power at different speeds at 2500 rpm, 5000 rpm. Presently used materials are Cast iron and Cast steel. For validating design Structural Analysis is also conducted by varying the materials for gears, Cast Iron and of Aluminum Alloy. The analysis is conducted to verify the best material for the gears in the gear box at higher speeds by analyzing stress, displacement and also by considering weight reduction.

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1. INTRODUCTION:

Originally, worm gearing was used to secure, by compact means, a large reduction of speed between driving and driven shafts with a proportionate increase (except for frictional loss) in the torque of the driven shaft. Worm gearing is still used for this purpose, and frequently the wheel is driven by a single-thread worm of such low helix angle that the drive cannot be reversed; that is the wheel cannot drive the worm as the gearing automatically locks itself against backward rotation. Although a multiple-threaded worm when applied under like conditions is much more efficient than a single-threaded worm, it does not follow that the multiple-threaded worm should always Be used. A single-threaded worm might be preferable when the most important requirement is to obtain a high ratio and especially if the worm must be self-locking.

When power is the primary factor, the multiplethreaded worms should be used. Lubrication is an important factor when using worm gearing. An increase in heat generated means a decrease in efficiency. The amount of power which can be transmitted at a given temperature increases as the efficiency of the gearing increases. Materials for worm and worm gears are generally confined to steel for worms and bronze or cast iron for gears. When steel worms are run with bronze gears at high speeds, the worm is usually hardened with ground threads. However, unlike a worm, a worm gear's diameter is usually much larger than the width of its face.



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Figure 1.1: worm and worm wheel



Figure 1.2: worm gear and worm wheel

1.3 CIRCULAR (LINEAR) PITCH:

With a worm, circular (also referred to as linear) pitch is a distance measured along the pitch line of the gear. It can be determined by measuring – with an ordinary scale – the distance between any two corresponding points of adjacent threads parallel to the axis. (See Figure 1.4) With a worm gear, circular pitch is a distance measured along the pitch circle of the gear. It can be determined by measuring – with an ordinary scale – the distance between any two corresponding points of adjacent teeth. As noted above, this measurement should be taken on the pitch circle, which is approximately halfway down a tooth. (See Figure 1.6)



Figure 1.5: Worm



Figure 1.6: Worm Gear

WORMS – THREAD DIMENSIONSNB:

The dimensions of a worm thread are important because they provide valuable information when determining a customer's needs. As noted earlier, a worm thread is the part of the worm that wraps (spirals) around the cylindrical base of the worm, similar to the way the threads of a screw are configured.

The following terms are used when describing the dimensions of a worm-thread:

- Addendum the part of the thread from the pitch line of the worm to the outer edge of the thread. (See Figure 1.7A)
- 2. Dedendum the part of the thread from the pitch line of the worm to the bottom of the thread. The dedendum is equal to one addendum plus the working clearance (defined below). (See Figure 1.7A)
- 3. Working Clearance the distance from the working depth (defined below) to the bottom of the thread.
- 4. Working Depth the space occupied by the mating worm gear tooth. It is equal to twice the addendum.
- 5. Whole Depth the distance from the bottom of the thread to its outside diameter.



Figure 1.7A: Drawing of Worm showing cross section and full view of the thread.

1.4 WORMS-PITCH DIAMETER:

The pitch diameter of a worm is the diameter of the pitch circle (the "imaginary" circle on which the worm and worm gear mesh). There is no fixed method for determining the pitch diameter of a worm. (See Figure 1.7B)



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Important:

Pitch diameters can vary, but sound engineering practice dictates that they be as small as possible for the most efficient performance. Why? A small pitch diameter reduces the sliding velocity and, therefore, the efficiency of the worm.

1.8 WORMS-PRESSURE ANGLE:

The pressure angle is the angle at which a force is transmitted from the worm thread to the worm gear tooth. It determines the relative thickness of the base and top of the thread. (See Figure 1.10)



1.9 WORMS-PHYSICAL DIMENSIONS:

When ordering special (made-to-order) worms, the pitch, pitch diameter, pressure angle, number of threads and hand should always be specified, as should the physical dimensions illustrated in 1.11.



Figure 1.11

Note:

Sometimes a pinhole through the hub is required (rather than a keyway). If this is the case, be sure to specify the pin dimensions and location.

WORMS GEARS-BASIC DIMENSIONS:

Here are definitions you need to know in order to determine the basic dimensions of worm gears. (See Figure 1.12)

- 1. Pitch Diameter the diameter of the pitch circle (which, you will remember, is the "imaginary" circle on which the worm and worm gear mesh.
- 2. Working Depth the maximum distance the worm thread extends into the tooth space of the gear.
- 3. Throat Diameter the diameter of the throat circle at the center line of the worm gear face (the lowest point on the tooth face).
- 4. Outside Diameter the largest diameter of the worm gear teeth. It is equal to the diameter of the outside circle.
- 5. Root Diameter the smallest diameter of the worm gear. It is equal to the diameter of the root circle.



Figure 1.12



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1.19 Failure of Gears:

Failure of gears may be classified into four categories:

- 1. Surface fatigue (pitting)
- 2. Wear
- 3. Plastic flow
- 4. Breakage

The appearance of the various distress and failure modes can differ between gears that have through hardened teeth and those that have surface hardened teeth. These differences result from the different physical characteristics and properties and from the residual stress characteristics associated with the surface hardened gearing.

Advantage of worms and worms gear:

- 1. Higher speed reduction could be secured; speed reduction could be secured up to 300: 1
- 2. Worm and worm gears operate silently
- 3. Worm and worm gears will have one characteristics i.e. self locking. Reverse movement will be restricted but this characteristic depends on lead angle and friction angle, we have discussed this concept in our discussion in previous post during study of worm and worm gear.
- 4. Worm and worm gear unit will be preferred to use if space is restricted as we have already discussed that worm and worm gear unit could be used for heavy speed reduction in compact space also.
- 5. Handsome output torque will be secured here with the application of worm and worm gear.

Disadvantage of worms and worms gear:

1. Manufacturing cost is heavy as compared with manufacturing cost of bevel gear

2.Cost of raw material to manufacture the worm and worm gear set will be quite high

3. Worm and worm gear set will have heavy power losses.

4. Efficiency will be low

5.If speed reduction ratio is large, worm teeth sliding action will create lots of heat

6.Lubrication scheduled must be strictly maintained for healthiness of worm and worm gear as this unit requires much lubrication for smooth working of gearbox.

3. DESIGN CALCULATIONS OF WORM GEAR 3.1 ALUMINUM ALLOY7475-T761

3.1 2400 rpm

3.1.1 Worm Gear Diameter of crown wheel = DG= 475mm Number of teeth on gear = TG = 50Number of helical teeth on shaft = TP = 6Module = m=DG/TG=475/50=9.5=10(according to stds) Diameter of shaft = $DP = m \times TP = 10x6 = 60mm$ Material used for both shaft and gear is aluminum alloy7475-T761 Brinell hardness number(BHN)=140 Pressure angle of teeth is 20° involute system Ø= 20° P=162BHP = 162x745.7w=120803.4w We know that velocity ratio V.R=TG/ TP= DG/DP= NP/NG V.R=TG/ TP=50/6=6.25 V.R = NP/NG6.25=2400/NG NG=384rpm For satisfactory operation of gears the number of teeth in the shaft must not be Less than $\frac{48}{\sqrt{1}+(vr)^2}$ where v.r=velocity ratio $=\frac{10}{\sqrt{1}+(6.25)^2}=7.5$ Since the shafts are at right angles therefore pitch angle for the shaft $\theta p1 = tan - 1(1/v.r)$ $= \tan(1/6.25)$ =9.0 Pitch angle of gear $\theta p2=90^{\circ}-9=81$

We know that formative number of teeth for shaft

TEP= TPsec $\theta p1=8sec9=6$

And formative number of teeth for gear

TEG= TGsec $\theta p2=50sec81=319.622$

Tooth form factor for the shaft



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y1P=0.154-0.912/ TEP, for 20° full depth involute system =0.154-0.912/ 8 =0.04

And tooth form factor for gear y1G=0.154-0.912/ TEG =0.154-0.912/ 319.622

=0.151

Since the allowable static stresses(σ O) for both shaft and gear is same (i.e σ O=172.33 Mpa) and y1P is less than y1G, therefore the shaft is weaker. Thus the design should be based upon the shaft

Allowable static stress(σ O) = σ u/3=517/3=172.33 Mpa σ u=ultimate tensile strength=517 Mpa

TANGENTIAL TOOTH LOAD(WT)

WT = ($\sigma O \ge Cv$).b.II.m. y1P((L-b)/L) Cv=velocity factor =3/3+v, for teeth cut by form cutters v=peripheral speed in m/s b=face width m=module=10 y1p=tooth form factor L=slant height of pitch cone = $\sqrt{(\frac{D_G}{2})^2 + (\frac{D_P}{2})^2}$ DG= pitch diameter of gear =475 DP= pitch diameter of gear =80

DP= pitch diameter of gear = $V = \frac{\pi Dp NP}{60 \times 1000}$ =10.048m/s Cv==3/3+10.048=0.229 L= $\sqrt{(\frac{475}{2})^2 + (\frac{80}{2})^2}$

=240.844

The factor (L-b/L) may be called as bevel factor For satisfactory operation of the bevel gears the face width should be from 6.3m to 9.5m

So b is taken as 9.5m

b= 9.5x10=95

WT = $(172.33 \times 0.229) \times 95 \times \Pi \times 10 \times 0.04 (\frac{240.844 - 95}{240.844})$ = 2922.51N

STATIC TOOTH LOAD (WS)

The static tooth load or endurance strength of the tooth for worm gear is given by

WS= $\sigma e.b.\Pi.m. y1P(\frac{L-b}{r})$

(Flexible endurance limit) $\sigma e = 1.75XB.H.N = 1.75X140=245$

WS=245 × 95 × π × 10 × 0.041 ($\frac{240.844-95}{240.844}$)

WS=18145N

For safety against tooth breakage the $~WS \ge 1.25 \ Wd = 13165.2875$

WEAR LOAD (WW)

The maximum or limiting load for wear for worm gears is given by

$$Ww = \frac{D_{P \times b \times q \times k}}{\cos \theta_{p1}}$$

Dp,b,q,k have usual meanings as discussed in worm gears except that Q is based on formative or equivalent no.of teeth such that ratio factor $Q = \frac{2T_{EG}}{T_{EG+T_{EP}}}$

$$=\frac{2\times319.622}{319.622+8}=1.951$$

K= load stress factor (also known as material combination factor)in N/mm2 given by

 $\mathrm{K} = \frac{\sigma_{es}^{2} \times \sin \emptyset}{1.4} \left(\frac{1}{E_{P}} + \frac{1}{E_{G}} \right)$

 σ es= surface endurance limit in mpa or N/mm2 $\emptyset = pressure \ angle$ σ es=(2.8×B.H.N-70)N/mm2

$$= (2.8 \times 517-70) = 322 \text{ N/mm2}$$

$$K = \frac{(322^2) \sin 20}{1.4} \left(\frac{1}{70300} + \frac{1}{70300}\right) = 0.72$$

$$\cos\theta_{p1} = \cos 9 = 0.987$$

$$Ww = \frac{80 \times 95 \times 1.951 \times 0.72}{0.987} = 10825.25\text{ N}$$

Forces acting

WT=WNCOS

WN=normal load=WT/ COS^{\emptyset} WT=tangential force WN= $\frac{tangential force}{COS \phi} = \frac{2922.51}{cos 20} = 3110.070$ N Radial force WR= $W_T tan \phi = 3110.070 tan 20 = 1131.972$



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Mean radius (Rm)=(L-b/2) $\sin \theta_{p1}$ =(240.844-95/2) $\sin 9$ =32.111

Axial force acting on the shaft shaft WRH=WT*tan* Ø sin θ P1 Tangential force acting at the mean radius WT=T/Rm T= torque on the shaft T = $\frac{p \times 60}{2\pi \times N_P}$ = $\frac{120803.4 \times 60}{2\pi \times 2400}$ T=480.661N-m=480661N-mm

WT=480661/32.111=14968.733N

Axial force WRH=WT $tan \phi sin \theta P1$ =14968.733tan 20 sin 9=850.010N Radial force acting on the shaft shaft WRH=WT $tan \phi cos \theta P1$ =14968.733tan 20 cos 9=5366.752N

TANGENTIAL TOOTH LOAD(WT)

WT =($\sigma O \ge Cv$).b. Π .m. y1P((L-b)/L) Cv=velocity factor =3/3+v, for teeth cut by form cutters v=peripheral speed in m/s b=face width m=module=7 y1p=tooth form factor L=slant height of pitch cone $= \sqrt{(\frac{D_G}{2})^2 + (\frac{D_P}{2})^2}$

DG= pitch diameter of gear =150mm Dp= pitch diameter of gear =70mm

 $V = \frac{\Pi Dp NP}{60 \times 1000}$

 $= \frac{\Pi \times 70 \times 2400}{60 \times 1000}$

=8.792m/s Cv==3/3+8.792=0.254 $L=\sqrt{\left(\frac{150}{2}\right)^2 + \left(\frac{70}{2}\right)^2}$ =82.764

The factor (L-b/L) may be called as bevel factor For satisfactory operation of the bevel gears the face width should be from 6.3m to 9.5m So b is taken as 9.5m b= 9.5x7=66.5WT =(172.33x0.254) $x66.5x\Pi x7x0.099(\frac{82.764-66.5}{82.764})$ =1244.7N

STATIC TOOTH LOAD (WS)

The static tooth load or endurance strength of the tooth for bevel gear is given by WS= $\sigma e.b.\Pi.m. y1P(\frac{L-b}{L})$ (Flexible endurance limit) $\sigma e = 1.75XB.H.N =$ 1.75X140 = 245WS= $245 \times 66.5 \times \pi \times 7 \times 0.099(\frac{82.764-66.5}{82.764})$ WS=6966.47N For safety against tooth breakage the WS ≥ 1.25 Wd=6892.2125 WS > Wd

WEAR LOAD (WW)

The maximum or limiting load for wear for bevel gears is given by

 $Ww = \frac{D_{P \times b \times q \times k}}{\cos \theta_{p1}}$

Dp,b,q,k have usual meanings as discussed in worm gears except that Q is based on formative or equivalent no.of teeth such that ratio factor $Q = \frac{2T_{EG}}{T_{EG+T_{EP}}}$

$$=\frac{2\times42.55}{42.55+16.554}=1.439$$

K= load stress factor (also known as material combination factor)in N/mm2 given by

$$K = \frac{\sigma_{es}^2 \times \sin \phi}{1.4} \left(\frac{1}{E_P} + \frac{1}{E_C}\right)$$

 σ es= surface endurance limit in mpa or N/mm2 \emptyset = pressure angle

σes=(2.8×B.H.N-70)N/mm2

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= (2.8×140-70)=322 N/mm2

$$K = \frac{(322^2)\sin 20}{1.4} \left(\frac{1}{70300} + \frac{1}{70300}\right) = 0.72$$

$$\cos\theta_{p1} = \cos 25.025 = 0.906$$

 $Ww = \frac{70 \times 66.5 \times 1.439 \times 0.72}{0.906} = 5322.62N$

Forces acting

WT=WNCOS

WN=normal load=WT/ COS^{\emptyset} WT=tangential force WN= $\frac{\text{tangential force}}{\cos \phi} = \frac{1244.7}{0.939} = 1324.582N$

Radial force WR=WT $tan\phi = 1324.582tan20 = 482.108N$

Mean radius (Rm)=(L-b/2)sin θ_{p1} =(82.764-66.5/2) sin 25.025 =20.944N

Axial force acting on the shaft shaft WRH=WTtan $\emptyset \sin \theta P1$

Tangential force acting at the mean radius WT=T/Rm

T= torque on the shaft $T = \frac{p \times 60}{2\pi \times N_{p}}$ $= \frac{120803.4 \times 60}{2\pi \times 2400}$ T=480.661N-m=480661N-mm

WT=480661/20.944=22949.818N

Axial force WRH=WTtan Ø sin θP1 =22949.818tan 20 sin 25.0259 =3533.340N Radial force acting on the shaft shaft WRH=WTtan $\emptyset \cos \theta P1$ =22949.818tan 20 cos 25.025

=22949.818tan 20 cos 25.0

=7567.863N

4. RESULTS TABLE 4.1 2400 RPM

TANGENTIAL	Aluminum Alloy	Cast Iron	
LOAD (N)	2922.51	3243.08	
DISPLACEMENT (mm)	0.0241696	0.0100566	
STRESS (N/mm2)	3.19018	3.57544	
STRAIN	4.1593e-5	1.69558 e-5	
STATIC			
LOAD (N)	18143.3	37933.7	
DISPLACEMENT (mm)	0.150063	0.11763	
STRESS (N/mm2)	19.8068	41.8212	
STRAIN	0.000258239	0.000198329	

5. INTRODUCTION TO CAD:

Computer-aided design (CAD), also known as computer-aided design and drafting (CADD), is the use of computer technology for the process of design and design-documentation. Computer Aided Drafting describes the process of drafting with a computer. CADD software, or environments, provide the user with input-tools for the purpose of streamlining design processes; drafting, documentation, and manufacturing processes. CADD output is often in the form of electronic files for print or machining operations. The development of CADD-based software is in direct correlation with the processes it seeks to economize; industry-based software (construction, manufacturing, etc.) typically uses vector-based (linear) environments whereas graphic-based software utilizes raster-based (pixelated) environments.





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5.2.22 ASSEMBLE OF WORM GEAR BOX IN EXPLODE VIEW



Lead Image Lead Image Force-1 Lead Image Lead Deck Force-1 Lead Image Pace(s) Type Apply sormal force Value: 292251N

6.2.1.2.4 Study Results



6.1 INTRODUCTION TO ANSYS

ANSYS is a useful software for design analysis in mechanical engineering. That's an introduction for you who would like to learn more about ANSYS WORKBENCH. ANSYS is a design analysis automation application fully integrated with Solid Works. This software uses the Finite Element Method (FEM) to simulate the working conditions of your designs and predict their behavior. FEM requires the solution of large systems of equations. Powered by fast solvers, ANSYS WORKBENCH makes it possible for designers to quickly check the integrity of their designs and search for the optimum solution.

6.2 STRUCTURAL ANALYSIS OF WORM GEAR

6.2.1 2400 rpm
6.2.1.2. ALUMINUM ALLOY
6.2.1.2.1 TANGENTIAL LOAD
6.2.1.2.2 Material Properties
6.2.1.1.7 Mesh Information – Details
6.2.1.2.3 Loads and Fixtures



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6.2.1.2.5 STATIC LOAD 6.2.1.2.6 Loads and Fixtures







6.2.1.2.7 Study Results





7. RESULTS TABLE 7.1 2400 RPM

		Aluminum	
S.NO.	TANGENTIAL	Alloy	Cast Iron
1	LOAD (N)	2922.51	3243.08
	DISPLACEMENT		
2	(mm)	0.00699	0.005145
3	STRESS (N/mm2)	40.096	45.084
4	STRAIN	5.79E-04	4.22E-04
5	STATIC		
6	LOAD (N)	18143.3	37933.7
	DISPLACEMENT		
7	(mm)	0.0434	0.0601
8	STRESS (N/mm2)	248.92	527.34
9	STRAIN	0.0035	0.0049





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8. CONCLUSION:

In our project we have designed a Worm gear box. Loads are calculated when the gears are transmitting different speeds 2400rpm and 5000rpm and different materials Aluminum Alloy and Cast Iron. By observing the structural analysis results using Aluminum alloy the stress values are within the permissible stress value. So using Aluminum Alloy is safe for differential gear. When comparing the stress values of the three materials for all speeds 2400rpm and 5000rpm, the values are less for Aluminum alloy than Cast Iron. And also weight of the Aluminum alloy reduces almost 3 times when compared with d Cast Iron since its density is very less. Thereby mechanical efficiency will be increased. By observing analysis results, Aluminum Alloy is best material for Differential.

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Cast Iron

Aluminum Alloy

MATERIAL



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