The design and efficient hardware implementations for the Advanced Encryption Standard (AES) algorithm in order to attain better FPGA efficiency.

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Abstract:
The Advanced Encryption Standard (AES) was endorsed by the National Institute of Standards and Technology in 2001. It was designed to replace the aging Data Encryption Standard (DES) and be useful for a wide range of applications with varying throughput, area, power dissipation and energy consumption requirements. Though they are highly flexible, FPGAs are often less efficient than Application Specific Integrated Circuits (ASICs); There have been many AES implementations that focus on obtaining high throughput or low area usage, but very little research done in the area of low power or energy efficient based AES; in fact, it is rare for estimates on power dissipation to be made at all.

This thesis introduces new efficient hardware implementations for the Advanced Encryption Standard (AES) algorithm. Two main contributions are presented in this thesis, the first one is a high speed 128 bits AES encryptor, and the second one is a new 32 bits AES design. In first contribution a 128 bits loop unrolled sub-pipelined AES encryptor is presented. In this encryptor an efficient merging for the encryption process sub-steps is implemented after relocating them. The second contribution presents a 32 bits AES design. In this design, the S-BOX is implemented with internal pipelining and it is shared between the main round and the key expansion units. Also, the key expansion unit is implemented to work on the fly and in parallel with the main round unit. These designs have achieved higher FPGA (Throughput/Area) efficiency comparing to previous AES designs.

Keywords— AES, Cryptography, Pipelined AES, Security, Encryption, Decryption

I. INTRODUCTION
The large and growing number of internet and wireless communication users has led to an increasing demand of security measures and devices for protecting the user data transmitted over the unsecured network so that unauthorized persons cannot access it. The increasing need for Secured data communication has led to development of several cryptography algorithms. Two types of cryptographic systems are mainly used for security purpose, one is symmetric-key crypto system and other is asymmetric-key crypto system. Symmetric-key cryptography (DES, 3DES and AES) uses same key for both encryption and decryption. The asymmetric-key cryptography (RSA and Elliptic curve cryptography) uses different keys for encryption and decryption. Symmetric crypto system has advantages over asymmetric crypto system. Symmetric key Algorithms are in general much faster to execute electronically than asymmetric key algorithms. Smaller key length is the major disadvantage of DES crypto system.

In November 2001, the National Institute of Standards and Technology (NIST) of the United States choose the Rijndael algorithm as the suitable Advanced Encryption Standard (AES) to replace previous algorithms like DES, 3DES algorithm. The AES encryption is considered to be efficient in both
hardware and software implementations. Compared to software, hardware implementation is more secured and reliable. Software implementation of AES algorithm is slower process so the focal approach of our design on hardware platform is to attain speed. So this paper addresses efficient hardware implementation of the AES (Advanced Encryption Standard) algorithm and describes the design and performance evaluation of Rijndael algorithm. A strong focus is placed on high throughput implementations, which are required to support security for current and future wide bandwidth applications. This implementation will be useful in wireless security like military communication, Cellular networks, Web servers, Mobile networks, Smart cards etc.

II. AES ALGORITHM

In cryptography, the Advanced Encryption Standard (AES), also known as Rijndael, is a block cipher adopted as an encryption standard by the US government. The cipher was developed by two Belgian cryptographers, Joan Daemen and Vincent Rijmen and submitted to the AES selection process under the name "Rijndael", a portmanteau comprised of the names of the inventors. AES is a symmetric iterative private key block cipher algorithm that can process data of different length say 128, 192 or 256 bits with a private key of same length. Each iteration in an algorithm is called as a round and it has 10, 12 or 14 rounds for processing data blocks of 128,192 or 256 bits respectively. The key could be generated and scheduled in each round to get the encrypted data. Table 1 shows the number of rounds as a function of key length.

**TABLE I. Different AES specifications**

<table>
<thead>
<tr>
<th>AES Version</th>
<th>Key Size (N bytes)</th>
<th>Block Size (N bytes)</th>
<th>Number of Rounds (Nr rounds)</th>
</tr>
</thead>
<tbody>
<tr>
<td>AES128</td>
<td>4</td>
<td>4</td>
<td>10</td>
</tr>
<tr>
<td>AES192</td>
<td>8</td>
<td>4</td>
<td>12</td>
</tr>
<tr>
<td>AES256</td>
<td>10</td>
<td>4</td>
<td>14</td>
</tr>
</tbody>
</table>

There are four basic operations carried out in each round of the AES algorithm, they are

i) Sub-byte
ii) Shift row
iii) Mixed column
iv) Add Round Key

The last round of the encryption alone is different in a way that the mixed column operation will not be carried out. A 128-bit data block is divided into 16 bytes and these 16 bytes are mapped as 4X4 matrix and each entry are called as states. These states undergo all mathematical operation carried out in each rounds of the AES algorithm. Every State variable is to considered in the element of GF(2). Although there are different irreducible polynomials that could be used for GF (28), this AES algorithm uses P(x) = x8 + x4 + x3 + x +1 as its irreducible polynomials. Decryption can be done by the inverse process of encryption operation. The AES encryption and the equivalent decryption structures are shown in Fig.1.

**Fig.1 Encryption and Equivalent Decryption Structure**

A. Sub bytes transformation

The Sub Bytes transformation is a non-linear byte substitution that operates independently on each byte of the State using a substitution table (S-box). This S-box which is invertible is constructed by composing two transformations:

1. Take the multiplicative inverse in the finite field GF (28), the element {00} is mapped to itself.
2. Apply the affine transformation over GF (2)
Similarly inverse sub bytes implemented by using inverse affine transform followed by multiplicative inverse.

B. Shift rows transformation
In the Shift Rows transformation, the bytes in the last three rows of the State are cyclically shifted over different numbers of bytes (offsets). The first row is not shifted at all, the second row is shifted by one the third row by two, and the fourth row by three bytes to the left. In the InvShiftRows, the first row of the State does not change, while the rest of the rows are cyclically shifted to the right by the same offset as that in the Shift Rows transformation.

C. Mixcolumns transformation
The MixColumns transformation operates on the State column-by-column, treating each column as a four-term polynomial. The columns are considered as polynomials over $GF(2^8)$ and multiplied modulo $x^4 + 1$ with a fixed polynomial $a(x)$, given by $a(x) = \{03\}x^3 + \{01\}x^2 + \{01\}x + \{02\}$. In hardware, the multiplication by the corresponding polynomial is done by XOR operations. In matrix form, the MixColumns transformation can be expressed as

$$\begin{bmatrix}
S'_0 & S'_1 & S'_2 & S'_3 \\
S_0 & S_1 & S_2 & S_3 \\
S_0 & S_1 & S_2 & S_3 \\
S_0 & S_1 & S_2 & S_3 \\
\end{bmatrix} =
\begin{bmatrix}
\{02\} & \{03\} & \{01\} & \{01\} \\
\{01\} & \{01\} & \{02\} & \{03\} \\
\{01\} & \{01\} & \{02\} & \{03\} \\
\{01\} & \{01\} & \{02\} & \{03\} \\
\end{bmatrix}
\begin{bmatrix}
S_0 & S_1 & S_2 & S_3 \\
\end{bmatrix}$$

Fig. 3 Mixcolumns transformation

The InvMixColumns multiplies the polynomial formed by each column of the State with $a^{-1}(x)$ modulo $x^4 + 1$, where $a^{-1}(x) = \{0b\}x^3 + \{0d\}x^2 + \{09\}x + \{0e\}$.

In matrix form, the InvMixColumns transformation can be expressed by

$$\begin{bmatrix}
S'_0 & S'_1 & S'_2 & S'_3 \\
\end{bmatrix} =
\begin{bmatrix}
\{0e\} & \{0b\} & \{0d\} & \{09\} \\
\{0d\} & \{09\} & \{0e\} & \{0b\} \\
\{0e\} & \{0b\} & \{0d\} & \{09\} \\
\{0d\} & \{09\} & \{0e\} & \{0b\} \\
\end{bmatrix}
\begin{bmatrix}
S_0 & S_1 & S_2 & S_3 \\
\end{bmatrix}$$

Fig. 4 Inverse Mixcolumns transformation

D. Addround key
In the add round key step the 128 bit data is XORed with the sub key of the current round using the key expansion operation. The add round key is used in two different places one during the start that is when round $r=0$ and then during the other rounds that is when $1 \leq \text{round} \leq \text{Nr}$, where $\text{Nr}$ is the maximum number of rounds. The formula to perform the add round key is

$$S'(x) = S(x) \oplus R(x)$$

$S'(x)$ – state after adding round key
$S(x)$ – state before adding round key
$R(x)$ – round key

III. KEY EXPANSION
In the AES algorithm, the key expansion module is used for generating round keys for every round. There are two approaches to provide round keys. One is to pre-compute and store all the round keys, and the other one is to produce them on-the-fly. In this paper it has been implemented with first approach. The key expansion has three steps:

- Byte Substitution subword()
- Rotation rotword()
- XOR with RCON (round constant)

The input to key schedule is the cipher key $K$. Key expansion generates a total of $\text{Nb} \times (\text{Nr} + 1)$ words. The algorithm requires an initial set of $\text{Nb}$ words, and each of the $\text{Nr}$ rounds requires $\text{Nb}$ words of key data. The resulting key schedule consists of a linear array of 4-byte words, denoted $[w_i]$, with $i$ in the range $0 \leq i < \text{Nb} \ (\text{Nr} + 1)$. 
The subword() function takes a four byte input and applies the byte substitution operation and produces an output word. The rotword() takes a word \([a0, a1, a2, a3]\) as input and performs a cyclic permutation to produce \([a1, a2, a3, a0]\) as output word. The round constant word array \(rcon[i]\) is calculated using the below formula in finite field.

\[Rcon[i] = x^{(2^{54+i})} \mod x^8 + x^4 + x^3 + x + 1\]

The first \(Nk\) words of the expanded key are filled with the cipher key. Every following word \(w[i]\) is equal to the xor of previous word \(w[i-1]\) and the word \(Nk\) positions earlier \(w[i-Nk]\). For words in positions that are a multiple of \(Nk\), a transformation is applied to \(w[i-1]\) prior to the XOR, followed by an XOR with a round constant \(rcon[i]\). This transformation consists of a cyclic shift of the bytes in a word rotword() and byte substitution subword(). But in key expansion of 256-bit cipher if \(Nk=8\) and \(i-4\) is a multiple of \(Nk\) then subword() function is applied to \(w[i-1]\) prior to the xor.

**IV. PIPELINING**

Rijndael is a block cipher with a basic looping architecture whereby data is iteratively passed through a round function. The architecture used in this implementation is shown in figure 5. In this architecture, Data to be encrypted/Decrypted and key is passed to the 2:1 multiplexer. In the starting the start signal is high mux performs xor between data and key, handover its output to further operation of AES.

![Fig. 5 Basic architecture of Design](image)

In most of the application Speed is very important factor. In order to speed up the AES algorithm we can use pipelining architecture. If we do the pipelining, Hardware gets doubled for each pipelining stage. Here we can implement the pipelining in each round of AES. For every pipelining stage throughput will increase, simultaneously power and area also increases. Increase in Throughput at the cost of increased area and power becomes a major drawback in nanometer technology. So we need to make a trade off while selecting the number of pipelining stages in the design. In this paper AES has been implemented with the different stages of pipelining. Throughput, Area and Power has been tabulated for all stages. Based on throughput requirement, number of pipelining stages can be restricted.

![Fig. 6 pipelining architecture](image)

In the above architecture, extra registers and hardware is repeated depending upon the number of pipelining stages so that, several blocks of data can be processed at a time as shown in figure 6.

**V. IMPLEMENTATION RESULTS**

The AES algorithm is implemented using Verilog.
hardware descriptive language and simulated using a Xilinx ISE 9.2 simulator. The algorithm is tested by encrypting and decrypting a single 128 bit block. Encryption simulation was successfully completed by the use of key expansion and transformations of shift Rows, sub bytes, mix columns, add round keys without pipelining stages shown in fig 7.

The Encryption block operating at an average frequency of 195 MHz for all pipelining stages and Decryption block operating at an average frequency of 226 MHz .The frequency has been calculated by synthesizing the design on virtex family. So, for throughput calculation 100 MHz clock has been considered as a reference. By looking at the TABLE II we can make out increase in number of pipelining stages leads to increase in area, power and Throughput. The synthesis results for Decryption block shown in the TABLE III.

TABLE II. Synthesis results of encryption Block

<table>
<thead>
<tr>
<th>Pipelining stages</th>
<th>Throughput</th>
<th>Area</th>
<th>Power dissipation</th>
<th>No of clock cycle</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>No of cells</td>
<td>Total area in mm²</td>
<td>Dynamic power in mW</td>
<td>Leakage power in mW</td>
</tr>
<tr>
<td>1</td>
<td>267</td>
<td>2.1462</td>
<td>7.0271</td>
<td>1.2827</td>
</tr>
<tr>
<td>2</td>
<td>369</td>
<td>3.5951</td>
<td>7.0901</td>
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</tr>
<tr>
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<td>457</td>
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<td>6.9795</td>
<td>1.0412</td>
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<tr>
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<td>1.3895</td>
</tr>
<tr>
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<td>4.9049</td>
<td>8.0837</td>
<td>1.2160</td>
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<tr>
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<td>5.7669</td>
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<td>13.0262</td>
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</tr>
<tr>
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<td>800</td>
<td>8.4268</td>
<td>14.0463</td>
<td>2.2413</td>
</tr>
</tbody>
</table>

Decryption simulation was successfully completed by the use of key expansion and transformations of inverse shift Rows, inverse sub bytes, inverse mix columns, inverse add round keys shown in fig 8.

The Different pipelining stage implementation of AES algorithm has been synthesized in RTL compiler using TSMC’s 180nm standard cells and corresponding variations in Throughput, Area, and Power for both Encryption and Decryption is tabulated .The synthesis results of an Encryption block shown in the TABLE II.

TABLE III. Synthesis results of Decryption Block

<table>
<thead>
<tr>
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VI. CONCLUSION

In this paper, we presented a hardware implementation of pipeline AES architecture which includes both encryption and decryption and also gives an idea of restricting the number of pipelining stages in the design. The design is modeled using Verilog HDL and simulated with the help of Xilinx ISE 9.2. Synthesis is done by using RTL Compiler v11.2. The encrypted cipher text and the decrypted text are analysed and proved to be correct for all the stages of pipelining.

REFERENCES


