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## Harmonic Reduction for Three Phase Voltage Source Inverters

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### **ABSTRACT:**

Sinusoidal Pulse Width Modulation (SPWM) and Space Vector Pulse Width Modulation (SVPWM) are the most popular modulation strategies for Multi level inverters. Two level inverters is the basic technique to implement any level. It becomes difficult in high voltage & high power applications due to the increased switching losses and limited rating of the dc link voltage. Multilevel inverters are used in high voltage and high power applications with less harmonic contents. This paper proposes a theoretical analysis and software implementation for two level SVPWM & three level SVPWM inverters and three-level SPWM inverters. This software implementation is performed by using MATLAB/SIMULINK software. This paper gives comparison between two level & three level inverters using SVPWM technique. Also this paper gives comparison between three level inverters using SVPWM and SPWM technique. The simulation study reveals that three-level SVPWM inverter generates less THD compared to two-level SVPWM inverters & Threelevel SPWM inverters

#### Key words:

SVPWM, SPWM, THD, TWO &THREE LEVEL IN-VERTERS

### **1. INTRODUCTION:**

In Sinusoidal Pulse width modulation (SPWM) we generate the gating signals by comparing sinusoidal reference signal with a triangular carrier wave. SVPWM (Space vector pulse width modulation) technique was originally developed as a vector approach to PWM for three phase inverters. It is an advanced computation method and it is quite different from reaming methods. The Space Vector PWM of a three level inverter provides the additional advantage of superior harmonic quality. As the number of voltage levels increases, the harmonic content of the output voltage waveform decreases significantly [6]. **Dr.L.Maheswari** 

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As the number of levels is increased, the amount of switching devices and other component are also increased, making the inverter becoming more complex and costly. In case of the conventional two level inverter configurations, the harmonic reduction of an inverter output is achieved by raising the switching frequency. However in the field of high voltage and high power applications, the switching frequency of the power device has to be restricted below 1 KHz due to the increased switching losses. So the harmonic reduction by raised switching frequency of two-level inverters becomes more difficult in high power applications. From the aspect of harmonic reduction and high Dc-link voltage level, three-level approach looks like a most alternative.

### 2.ANALYSIS OF TWO LEVEL INVERT-ERS:



## Figure.1 Three-Phase two level voltage source inverters

Space Vector Modulation (SVM) is a more sophisticated technique for generating sine wave that provides higher voltages with lower total harmonic distortion. The circuit model of a typical three-phase two level voltage source PWM inverter is shown in "Figure.1". S1 to S6 are the six power switches [2] that shape the output. When an upper transistor is switched on, i.e. when a, b or c is 1 and the corresponding lower transistor is switched on, i.e. the corresponding a', b' or c' is zero. Therefore, the on and off states of the transistors can be used to determine the output voltage. If two switches, one upper and one lower switch conduct at the same time such that the output voltage is  $\pm$ , the switch state is 1. If these two switches are off at the same time, the switch state is 0.



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### A .SWITCHING STATES:

The total number of switching states in an "N" level inverter is "N3". So the total number of switching states in a "2" level inverter is "23" that is 8 switching states. They are S0, S1, S2, S3, S4, S5,S6, and S7. S0 and S7 are called as zero switching states because during which there is no power flow from source to load.S1 to S6 are called as active switching states.



#### Figure.2 Switching states of two level inverters [5]

### **B**.SPACE VECTOR DIAGRAM:



Figure.3 Space vector diagram of two level inverters [5] Space vector diagram is divided into six sectors. The duration of each sector is 600. V1, V2, V3, V4, V5, V6 are active voltage vectors and V0 & V7 are zero voltage vectors. Zero vectors are placed at origin. The lengths of vectors V1 to V6 are unity and lengths of V0 and V7 are zero. The space vector Vs constituted by the pole voltage , and is defined as [3]

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 \begin{split} & V_{s} = V_{ao} + V_{bo} e^{j(z\pi/3)} + V_{co} e^{j(\pi/3)} \\ & V_{ao} = V_{an} + V_{no}, \quad V_{bo} = V_{bn} + V_{no} \\ & V_{co} = V_{cn} + V_{no} \\ & V_{an} + V_{bn} + V_{cn} = 0, \quad V_{no} = (V_{ao} + V_{bo} + V_{co})/3 \\ & V_{ab} = V_{ao} - V_{bo}.V_{bc} = V_{bo} - V_{co} & V_{ca} = V_{co} - V_{ao} \\ & FOR example voltage vector V_1 that is 100 \\ & V_{ao} = V_{dc}.V_{bo} = 0 & V_{co} = 0 \\ & V_{no} = (V_{dc} + 0 + 0)/3 = (V_{dc}|3) \\ & V_{an} = V_{ao} - V_{no} = (2|3) V_{dc} \\ & V_{bn} = V_{bo} - V_{no} = (-1|3) V_{dc} \\ & V_{ab} = V_{ao} - V_{bo} = V_{dc}, \quad V_{bc} = V_{bo} - V_{co} = 0 \\ & V_{ac} = V_{co} - V_{ao} = -V_{dc} \end{split}
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# TABLE.I: SWITCHING VECTORS, PHA-<br/>SEVOLTAGES, OUTPUT VOLTAGES [2]



(Note: Respective voltages should be multiplied by Vdc)

### **3. ANALYSIS OF 3 LEVEL I NVERTERS**



Figure.4. Three Phase three level voltage source inverters The circuit [1] employs 12 power switching devices and 6 clamping diodes. Each arm containsfour IGBTs, four anti parallel diodes and two neutral clamping diodes. And the dc bus voltage is split into three levels by two series connected bulk capacitors C1, C2 two capacitors have been used to divide the DC link voltage into three voltage levels, thus the name of 3-level. The middle point of the two capacitors can be defined as the neutral point 0.

## TABLE.II:THE SWITCHING VARIABLESOF PHASE A [3]

Vao	Sal	S <sub>a2</sub>	S <sub>a3</sub>	S <sub>a4</sub>	Sa
$+V_{dc}/2$	1	1	0	0	2
0	0	1	1	0	1
$-V_{dc}/2$	0	0	1	1	0



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Figure 5 Space Vector Diagram of Three Level Inverters

The plane can be divided into 6 majortriangular sectors (I to VI) by large voltage vectors and zero voltage vectors. Large voltage vectors are V13, V14, V15, V16, V17, and V18. Medium voltage vectors are V7, V8, V9, V10, V11, and V12. Small voltage vectors are V1, V2, V3, V4, V5, and V6. Zero voltage vectors are V0.Phase angle  $\alpha$  is calculated and then sector, in which the command vector V\* is located, is determined as: If  $\alpha$  is between  $0 \le \alpha < 60^\circ$ , and V\* will be in major sector II. If  $\alpha$  isbetween  $120^\circ \le \alpha < 120^\circ$ , and V\* will be in major sector III. If  $\alpha$  is between  $180^\circ \le \alpha < 240^\circ$ , and V\* will be in major sector III. If  $\alpha$  is between  $180^\circ \le \alpha < 240^\circ$ , and V\* will be in major sector IV. If  $\alpha$  is between  $240^\circ \le \alpha < 300^\circ$ , and V\* will be in major sector V. Will be in major sector V. If  $\alpha$  is between  $300^\circ \le \alpha < 360^\circ$  and V\* will be in major sector VI.

### **B. REGION IN A PARTICULAR SECTOR:**

For example we are taking the space vector diagram of sector I for determining the particular region in a sector 1. Sector I contains 4 minor triangular sectors. D1, D7, D13 and D14 are 4 minor triangular sectors. In each of the four minor regions, the reference vector is located in one of the 4 regions, where each region is limited by three adjacent vectors. Then

 $V_{ref} = V^* = V_x(T_x/T_s) + V_y(T_y/T_s) + V_z(T_z/T_s)$   $T_x/T_s + T_y/T_s + T_z/T_s = 1$   $T_x/T_s = X, T_y/T_s = Y \text{ and } T_z/T_s = Z$   $T_x + T_y + T_z = T_s$ Based on the principle of vector synthesis, the following equations can be written as: X + Y + Z = 1  $V_x X + V_y Y + V_z Z = V^*$ Modulation ratio  $M = \frac{V^*}{(2|3)V_{dc}} = (3V^*|2V_{dc})$ As shown in figure 5, the boundaries of modulation ratio are Mark1, Mark 2, and Mark3 [1].

$$Mark1 = \frac{\sqrt{3}/2}{\sqrt{3}\cos\theta + \sin\theta}$$

$$Mark2 = \frac{\sqrt{3/2}}{\sqrt{3}\cos\theta - \sin\theta}, \theta \le \pi/6$$
$$= \frac{\sqrt{3}/4}{\sin\theta}, \frac{\pi}{6} < \theta \le \frac{\pi}{3}$$
$$Mark3 = \frac{\sqrt{3}}{\sqrt{3}\cos\theta + \sin\theta}$$

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TABLE III SWITCHING STATES OF 3 LEVEL INVERTERS [1]

Switching states	Sa	Sb	Se	Voltage Vectors
S1	0	0	0	V <sub>0</sub>
S2	1	1	1	V <sub>0</sub>
S3	2	2	2	V <sub>0</sub>
S4	1	0	0	V1
S5	1	1	0	V2
S <sub>6</sub>	0	1	0	V3
S7	0	1	1	V4
S <sub>8</sub>	0	0	1	V5
Sg	1	0	1	V <sub>6</sub>
S10	2	1	1	V <sub>7</sub>
S11	2	2	1	V <sub>8</sub>
S12	1	2	1	V <sub>9</sub>
S13	1	2	2	V10
S14	1	1	2	Vii
S15	2	1	2	V12
S <sub>16</sub>	2	1	0	V13
S17	1	2	0	V14
S18	0	2	1	V15
S19	0	1	2	V16
S <sub>20</sub>	1	0	2	V17
S <sub>21</sub>	2	0	1	V18
S22	2	0	0	V19
S23	2	2	0	V20
S <sub>24</sub>	0	2	0	V21
S <sub>25</sub>	0	2	2	V22
Sa26	0	0	2	V23
S27	2	0	2	V24

### **C.SWITCHING TIME PERIOD**

1) When the modulation ratio M < Mark1, then the rotating voltage vector V\* will be in sector D1 (Region 1). In a three level inverter, switching time calculation is based on the location of reference vector with in a sector. As shown in figure.5, is synthesized by V0, V1, and V2. In sector D1, the length of zero voltage vector V0 is zero & length of large voltage vector is 1.

$$\begin{split} V^*T_s &= V_1(T_1/T_s) + V_2(T_2/T_s) + V_0(T_0/T_s) \\ V_1X + V_2Y + V_0Z = V^* \\ V^* &= M(\cos\theta + j\sin\theta) \\ V_1 &= 1/2, V_2 = 1/2 \ (\cos 60^\circ, + j\sin 60^\circ) \& V_0 = 0. \\ M(\cos\theta + j\sin\theta) = \frac{1}{2} X + \frac{1}{2} \ (\cos 60^\circ + j\sin 60^\circ) Y \ (1) \\ X + Y + Z = 1 \ (2) \\ Using (1) \& (2), we can obtain X, Y \& Z \end{split}$$

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$$\begin{cases} X = 2m \cdot \left[ \cos \theta - \frac{\sin \theta}{\sqrt{3}} \right] \\ Y = m \cdot \frac{4 \sin \theta}{\sqrt{3}} \\ Z = 1 - 2m \left[ \cos \theta + \frac{\sin \theta}{\sqrt{3}} \right] \\ 2) \text{ Similarly when the modulation ratio Mark1\theta < 30^\circ$$
, then V\* will be in sector D<sub>13</sub>   
 V\*T\_s = V\_1(T\_1/T\_s) + V\_{13}(T\_{13}/T\_s) + V\_7(T\_7/T\_s) \\ V\_1X + V\_{13}Y + V\_7Z=V^\* \qquad (4) \\ \text{Using (4) & (2), we can obtain X, Y&Z \\} \begin{cases} X = -1 + 2m \left[ \cos \theta - \frac{\sin \theta}{\sqrt{3}} \right] \\ Y = m \cdot \frac{4 \sin \theta}{\sqrt{3}} \\ Z = 2 - 2m \left[ \cos \theta + \frac{\sin \theta}{\sqrt{3}} \right] \end{cases} \\ 4) \text{ When the modulation ratio Mark2 < M < Mark3 and  $0 < \theta < 30^\circ$ , then V\* will be in sector D<sub>13</sub>   
 V\*T\_s = V\_1(T\_1/T\_s) + V\_{13}(T\_{13}/T\_s) + V\_7(T\_7/T\_s) \\ V\_1X + V\_{13}Y + V\_7Z=V^\* \qquad (5) \\ \text{Using (5) & (2), we can obtain X, Y&Z \end{cases} \\ \begin{cases} X = 2m \left[ \cos \theta - \frac{\sin \theta}{\sqrt{3}} \right] \\ Y = m \cdot \frac{4 \sin \theta}{\sqrt{3}} \\ Z = 2 - 2m \left[ \cos \theta - \frac{\sin \theta}{\sqrt{3}} \right] \end{cases} \end{cases}

$$\begin{cases} X = 2m \left[ \cos \theta - \frac{1}{\sqrt{3}} \right] \\ Y = -1 + m \cdot \frac{4 \sin \theta}{\sqrt{3}} \\ Z = 2 - 2m \left[ \cos \theta + \frac{\sin \theta}{\sqrt{3}} \right] \end{cases}$$

### 4. ANALYSIS OF 3 LEVEL SPWM:

The sinusoidal PWM compares a high frequency triangular carrier with three sinusoidal reference signals, knows as the modulating signals, to generate the gating signals for the inverter switches. This is basically an analog domain technique and is commonly used in power conversion with both analog and digital implementation. By comparing a sinusoidal reference signal with a triangular carrier wave of frequency, gating signals are generated. The frequency of reference signal determines the inverter output frequency and its peak amplitude controls the modulation index M and then in turn the RMS output voltage. The number of pulses per half cycle depends on the carrier frequency. Within the constraint that two transistors of the same arm cannot conduct at the same time. Sinusoidal pulse width modulation [2] is used to control the inverter output voltage and maintains good performance to synthesize AC voltage wave forms in several applications, such as uninterruptible power supplies, motor drives and active filters.

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Figure .6 waveforms of SPWM

Inverter output voltage has the following features

1) PWM frequency is same as the frequency of trigging voltage Vtr.

2) Amplitude is controlled by the peak value of control voltage Vcnt

3) Fundamental frequency is controlled by the frequency of control voltageVcnt...

There are three sinusoidal reference waves

(,, Vrc) each shifted by 1200. A carrier wave is compared with the reference signal corresponding to a phase to generate the gating signals for that phase. Comparing the carrier signal () with the reference

### 5. SIMULATION MODELS:

S/FMI carbol block



2- level SVPWM Inverters

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Figure.18THD of SPWM 3 level inverter load voltage

	Vab	Vab	Inverter
Туре	Inverter	Load	current
	voltage	voltage	
SVPWM TWO LEVEL INVERTER	38.74%	13.12%	11.80%
SVPWM THREE LEVEL INVERTER	12.27%	6.19%	4.86%
SPWM THREE LEVEL INVERTER	35.89%	8.58%	6.56%

TABLE.IV COMPARISION OF SVPWM & SPWM INVERTER

#### TABLE.V SIMULATION PARAMETERS FOR TWO LEVEL & THREE LEVEL SVPWM INVERTER

Input DC link voltage for 2 level inverter	400V
Input DC link voltage ( $V_{dc1}$ ) for 3 level	
inverter	200V
Input DC link voltage ( $V_{dc2}$ ) for 3 level	
inerter	200V
Input voltage for 2 & 3 level inverter	400V
Fundamental frequency (F) for 2 & 3	
level inverter	50HZ
Switching frequency $(F_{\delta})$ for 2 & 3 level	
inverter	1000 HZ
	Ratio on
Transformer for 2 & 3 level inverter	Transformer
	(208/208V
	1KVA)
Three phase ac RL load Active power for	
2 & 3 level inverter	1kw
Three phase ac RL load	
Reactive power	500KVAR

### 6. CONCLUSION:

This paper work provides successfulattempt to analysis & comparison of SVPWM &SPWM inverters. In this paper, SVPWM strategy for two level & three level inverters and SPWM strategy for three level inverters is reported. From this paper SVPWM strategy concludes that, it generates less THD compared to SPWM strategy and also this paper concludes that when the number of levels increasing, harmonics are reduced for same technique as well as for different techniques. Simulation results have been given for R-L load in this paper. This software implementation used in this paper can be extended further to three phase Induction Motor load which will be a future enhancement. The proposed scheme is used for future works with high levels that is more than three level inverters.

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