

Sign detection algorithm using carry look ahead adder for the RNS Module Set $2n+1, 2n-1, 2n$.

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ABSTRACT: *The Residue Number System (RNS) is a non-weighted system that is very efficient in digital signal processing and communicational applications. The previous proposed methods for the residue to binary (R/B) conversions are based on the Chinese Remainder Theorem (CRT) or Mixed Radix Conversion (MRC). These theorems are difficult to implement. In this paper, we present a new high-speed ROM-less residue to binary converter for the three moduli set of $\{2n-1, 2n, 2n+1\}$. Our technique unlike previous methods uses the grouping numbers in dynamic representation range M which its delay is much less than other converters.*

Keywords: *residue number system, reverse converter, moduli set $\{2n-1, 2n, 2n+1\}$, group number.*

INTRODUCTION:

Residue Number System is an unconventional system. In this system, an integer X is represented by its remainder modulo a number of different bases. These residue numbers are smaller than the original number in the conventional system, so computations can be done with more speed and low power [1]. The advantages of RNS for implementing digital signal processors for certain applications such as FIR filtering are well-known [2-5]. Some of the more recent applications have been for 1-D filtering [6-8], 2-D filtering [9], video filtering [10], RSA cryptography [11-14], Elliptic curve cryptography [15], m -ary orthogonal keyed communication scheme [16], general purpose RISC DSP [17] and Image processing [18]. The RNS is determined using a set of relative pair wise prime integers positive co-prime integers $\{m_1, m_2, \dots,$

$m_n\}$ as moduli set. The dynamic range M of that system is given as a product of the moduli m_i where 1 can be uniquely—Any integer X between 0 and M represented as (x_1, x_2, \dots, x_n) . The residues $\| m_i$ $X_{x=i}$ also called residue digits, are defined as (2) $m_i x_{ii} \leq x_i < m_i + 1$. The two most important issues for the residue arithmetic are the choice of moduli sets and the conversion of residue to binary numbers. The choice of moduli set in RNS is of continuing interest. Early designs of RNS based processors were largely based on ROMs which used small set of mutually prime integers to realize a large dynamic range. However, the R/B converters for the general moduli sets are hardware intensive and implemented based on LUTs (Look-up tables). The access time of the LUTs and the need to read these iteratively have made the implementations inefficient for ASIC realization for RNS with large dynamic range. Hence, the more recent trend has been to use moduli sets which can help to eliminate the ROMs. These are known as power-of-two related moduli sets or “conversionfriendly” moduli sets [19].

Existing System:

It performed efficiently with limited amount or even without ROM. The periodicity properties exhibited by three moduli of this RNS result in superb performance of the binary to residue converter and modulo addition even for large n [27].

Section 2 describes how the conversion of RNS to binary system using the new approach. Section 3 presents the hardware implementation and in section 4, the proposed design is compared with other reported converters.

Proposed System:

For residue to binary conversion in moduli set $\{2n - 1, 2n, 2n + 1\}$, we distribute the numbers in dynamic representation range M into several groups and subgroups which a part of this novel idea is presented in [28]. Since, residue representation of X in above moduli set is corresponding with (x_1, x_2, x_3) , then the three residues denotes as:

$$x_1 = X \bmod 2^n - 1 = \underbrace{x_{1,n-1}x_{1,n-2} \dots x_{1,0}}_n$$

$$x_2 = X \bmod 2^n = \underbrace{x_{2,n-1}x_{2,n-2} \dots x_{2,0}}_n$$

$$x_3 = X \bmod 2^n + 1 = \underbrace{x_{3,n}x_{3,n-1} \dots x_{3,0}}_{n+1}$$

So, the group number of any residue number in the considered moduli set obtains according to Figure 1.

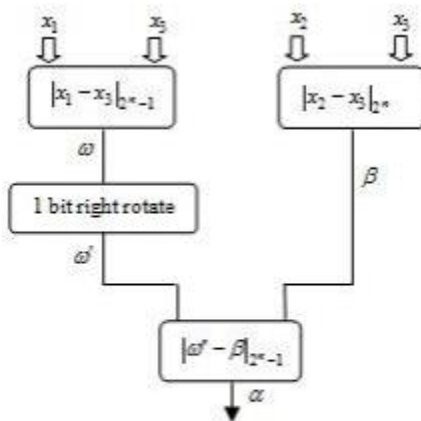


Fig. 1 Group Number Detection.

Table 1: Distribution of Numbers in subgroups

Number	Subgroup
$0 \rightarrow 2^n$	0
$2^n + 1 \rightarrow 2(2^n + 1) - 1$	1
$2^n(2^n + 1) \rightarrow 3(2^n + 1) - 1$	2
\vdots	
$(2^n - 1)(2^n + 1) \rightarrow 2^n(2^n + 1) - 1$	$2^n - 1$

$$g = |x_1 - x_3|_{2^{n-1}} \Rightarrow \begin{cases} 0 \leq X < 2^n + 1, & \omega = 0 \\ 2^n + 1 \leq X < 2(2^n + 1), & \omega = 2 \\ 2(2^n + 1) \leq X < 3(2^n + 1), & \omega = 4 \\ \vdots & \\ (2^{n-1} - 1)(2^n + 1) \leq X < 2^{n-1}(2^n + 1), & \omega = 2^n - 2 \\ 2^{n-1}(2^n + 1) \leq X < (2^{n-1} + 1)(2^n + 1), & \omega = 1 \\ \vdots & \\ (2^n - 2)(2^n + 1) \leq X < (2^n - 1)(2^n + 1), & \omega = 2^n - 3 \\ (2^n - 1)(2^n + 1) \leq X < 2^n(2^n + 1), & \omega = 0. \end{cases} \quad (7)$$

According to (7) and with regard to the product result from moduli subtraction in each group be appeared first, odd values and afterward even respectively. Since, in order to accomplishment of arithmetic operations should values increasingly, so it is achievable to be arranged the $\omega = 0, \omega$ through one bit right rotate. Therefore, if assume $2, 4, 6, \dots, 2n - 2, 1, 3, \dots, 2n - 3$, after 1-bit right rotate, $\omega = 0, 1, 2, \dots, 2n' \omega$ get $-3, 2n - 2$.

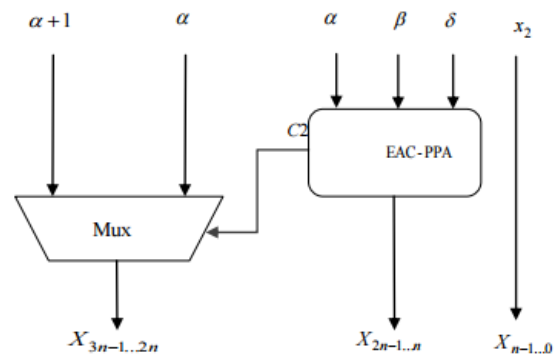


Fig. 2 reverse conversion unit

Hardware Structure

The group detection function is determined by Eq.(8) as $|x_1 - x_3|_{2^{n-1}} = \alpha \omega \beta -'$ is computed. According to [28], since α as a residue modulo $2n - 1$ then, instead of subtracting $12 - n\beta$ we can add its additive inverse modulo $2n - 1$. An additive inverse modulo $2n - 1$ is simply a negation of binary representation.

Proposed method for the numbers conversion from residue system to binary system is implemented with parallel prefix structure including parallel-prefix adder and end-around-carry prefix adder, both of which are

introduced in [29]. A parallel prefix adder and also parallel prefix adder with end-around-carry are built from elements shown in Figure 3.

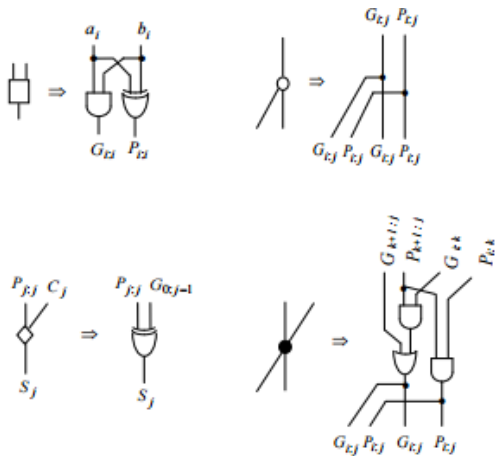


Fig. 3 Blocks of prefix adder structure [30].

The signals $G : ji$ and $P : ji$ are the carry generation and propagation functions from the position i to j . For an addition of two binary vectors $-01 n \dots aa$ and $-01 n \dots bb$ and for jki, \ll these functions can be expressed by logic equations

$$\begin{aligned} G_{i,j} &= a_i \cdot b_i \\ P_{i,j} &= a_i \oplus b_i \\ G_{i,j} &= G_{i,k} \cdot P_{k+1,j} + G_{k+1,j} \\ P_{i,j} &= P_{i,k} \cdot P_{k+1,j} \end{aligned}$$

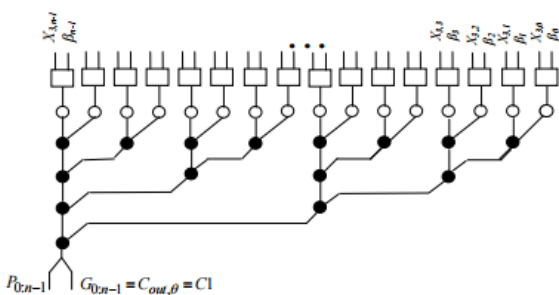


Fig. 4. Carry Generation Unit for $n=16$

The carry generation unit use $(n - 1)$ black nodes and n input nodes (denoted as square). Its area and time can be expressed as

$$\begin{aligned} A_2 &= 3n + 3(n-1) = 6n - 3 \\ T_2 &= 2 \log_2 n + 2 \end{aligned} \quad (27)$$

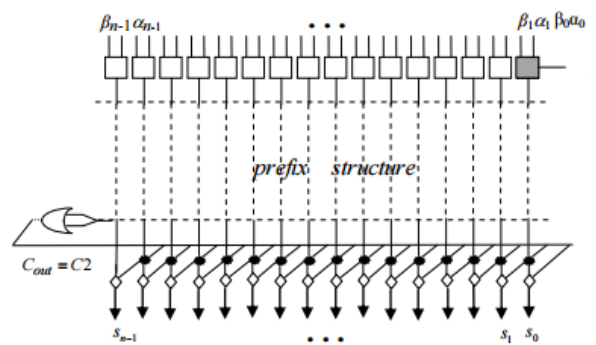


Fig. 5 EAC-PPA

The requirements for the above adder is as follows: n input nodes, n output nodes (denoted as lozenge), $(n - 1)$ black node, one additional gate. Notice that first input node is a full adder with area of 4 unit and delay of 2 unit more than half adder. The prefix part of circuit from [29] requires the delay of $\log_2 2n$ logic levels and also, the area of $\log_2 2n/3 (2nn)$. The AT parameters for the shown circuit in Figure 5

$$\begin{aligned} A_3 &= 8n + \frac{3}{2} n \log_2 n + 2 \\ T_3 &= 2 \log_2 n + 8. \end{aligned}$$

It is shown in EAC-PPA circuit that delay of generation of $C2$ is equal to $6\log_2 n + 17$. According to Fig. 2, the most significant n bits of $X + 1$. The output carry α or α binary system is given by signal from the circuit shown in Fig. 5 be called $C2$ is α selecting line of multiplexer which determine whether $+ 1$. In order to computation of α be directed to output or $, be \alpha + 1$, is sufficient after the value determination of α add with 1. $+ 1$ perform the function of α Therefore, the circuit adding 1 to a n -bit input number. Consider $0+1=en-1en-2... e1e0.\alpha1\alpha n-2... \alpha n-1\alpha+1=\alpha0,\alpha1\alpha n-2... \alpha n-1\alpha=\alpha$ We have the following equation, which imply that the circuit plus 1 requires $n-1$ XOR gates and n AND gates plus 1 inverter. $0\alpha e0= \oplus 1\alpha, e1=0,\alpha1\alpha$

Conclusions

Reverse converter is one of the most important issues in residue number system. In this paper, a novel and

fast algorithm for the conversion of numbers given in RNS $\{2n -1, 2n , 2n +1\}$ is presented. Our proposed technique is based on grouping numbers which has significant reduction in delay, compared to other methods. Furthermore, it accomplishes reverse conversion without applying the generic approaches such as CRT and MRC.

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